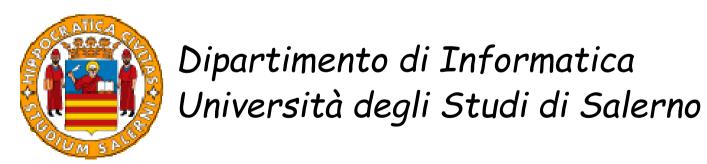
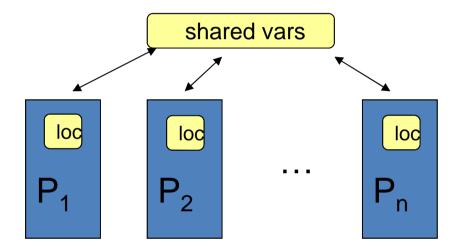
Analysis of Concurrent Programs via Sequentializations

Salvatore La Torre



Concurrent (shared-memory) Programs

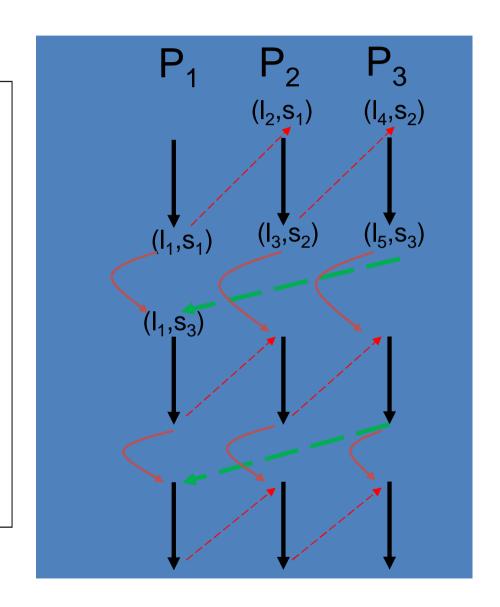
• Formed of sequential programs P_1, \ldots, P_n (each possibly with recursive function calls)



- Each program P_i can read and write shared vars
- We assume sequential consistency (writes are immediately visible to all the other programs)
- An execution is an interleaving of the executions of each program P_i

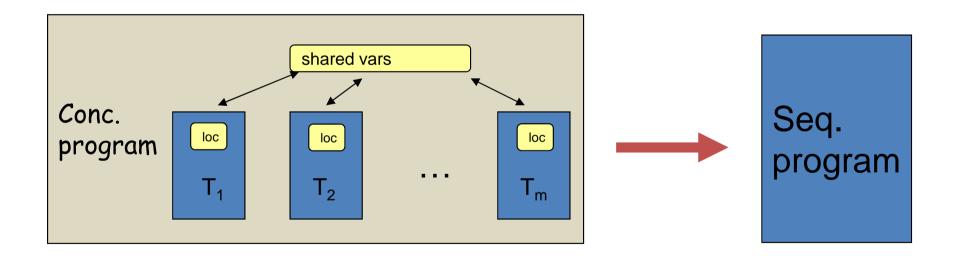
A concurrent execution (n=3)

- Programs are round-Robin scheduled in several rounds
 - round: formed of a context of each program
 - context: portion of run of a Pi
 - context-switch: active thread changes (global state is passed on to the next scheduled thread)
 - context-switching back to a thread resumes its local state

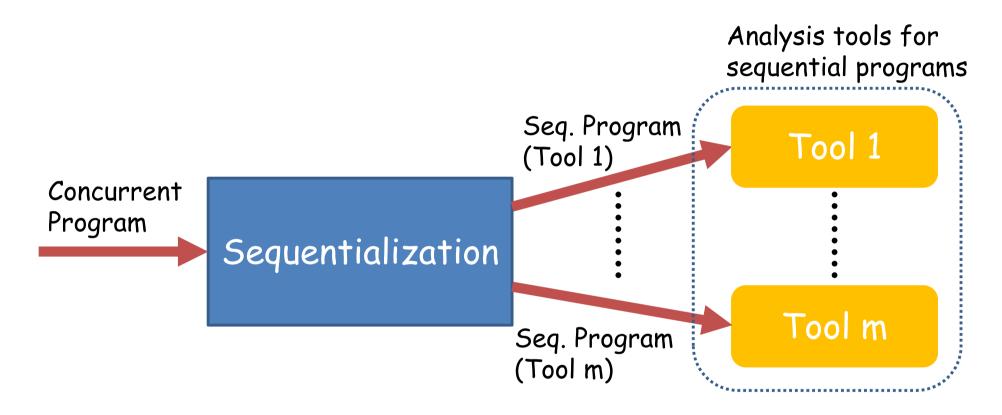


Sequentialization

 Code-to-code translation from a multithreaded program to an "equivalent" sequential one



Why sequentializing?



- Re-use of existing tools (delegate the analysis to the backend tool)
- Fast prototyping (designers can concentrate only concurrency features)
- Can work with different backends

Is this practical?

- Sequentializations inject control code in the original program
 - this can cause some overhead
 - performances of different translations may differ depending on the backend technology
- In the software verification competition (concurrency category) held at TACAS 2014, gold and silver medal went to tools using sequentializations
 - Lazy-CSeq and MU-CSeq
 (will be described in the talk of June 5)

Some general observations

- Sequentialization is always possible using unbounded resources
 - Sequential program keeps the call-stacks and just exectutes threads in time-sharing for any scheduling
- Efficient sequentialization yields an under-approximation of the concurrent programs
 - use prioritized search strategies (e.g., bounded contextswitching [Qadeer-Rehof, TACAS'05])
- Full coverage of the state space in very few cases
 - e.g., program abstractions with only two threads sharing only locks acquired/released under contextual locking [Chadha-Madhusudan-Viswanathan, TACAS'12]

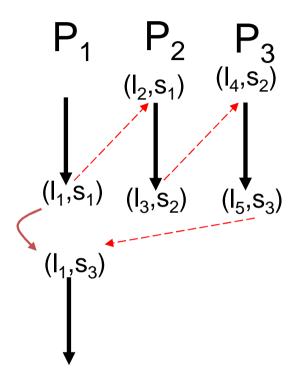
Outline

- First sequentialization
- Bounded context-switching
 - -Eager approach
 - -Lazy approach
- More sequentializations
- Conclusions

A first sequentialization

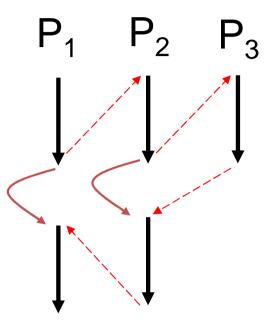
- KISS: Keep It Simple and Sequential (Microsoft tool) [Quadeer-Wu, PLDI'04]
- At context-switches either:
 - the active thread is terminated or
 - a not yet scheduled thread is started (by calling its main function)
- When a thread is terminated either:
 - the thread that has called it is resumed (if any) or
 - a not yet scheduled thread is started

Example (n=3)



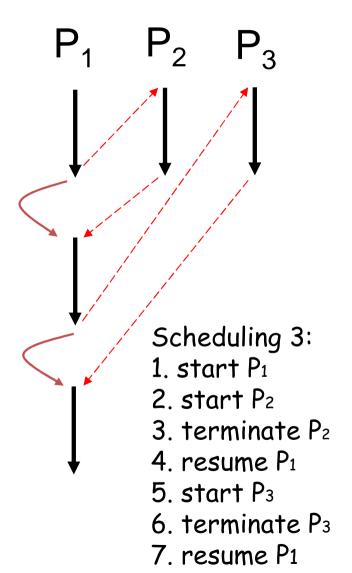
Scheduling 1:

- 1. start P₁
- 2. start P2
- 3. terminate P2
- 4. start P₃
- 5. terminate P₃
- 6. resume P₁



Scheduling 2:

- 1. start P₁
- 2. start P2
- 3. start P3
- 4. terminate P₃
- 5. resume P2
- 6. terminate P2
- 7. resume P₁



More on KISS

- Allows dynamic thread allocation in form of asynchronous calls
- Bounds the number of threads that have been created but not started yet
 - Scheduler starts a thread from this set (choosing it nondeterministically) or resumes the last suspended thread (if any)
- Used for assertion checking

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Bounded context-switching

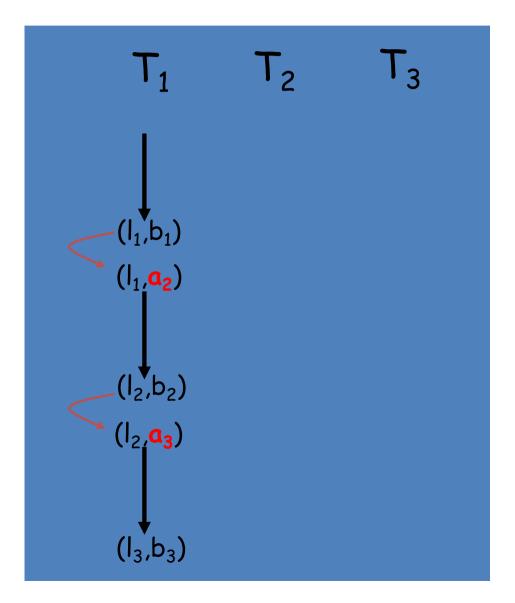
 Switching between threads is allowed only a bounded number of times [Qadeer-Rehof, TACAS'05]

Under this restriction

- Analysis is an effective technique for bug detection
 - bugs of concurrent programs are likely to occur within few context-switches [Musuvathi-Qadeer, PLDI'07]
 - Efficient sequentializations can be obtained
 - 1. Eager approach [Lal-Reps, CAV'08]
 - 2. Lazy approach [La Torre-Madhusudan-Parlato, CAV'09]

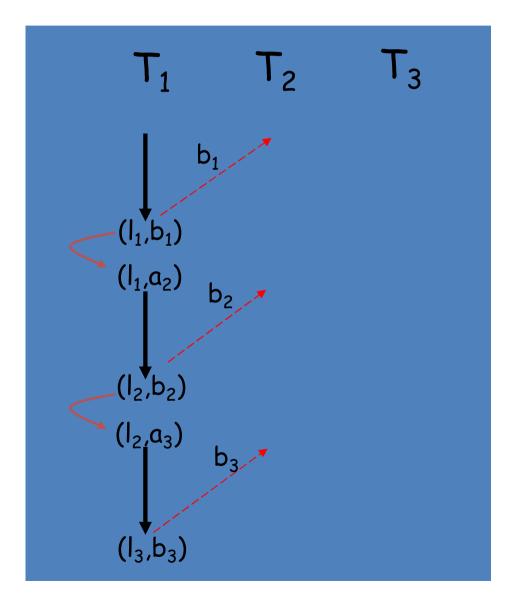
• [Lal-Reps, CAV'08]

- 1. Guess a_2, \ldots, a_k
- 2. Execute T₁ to completion
 - Computes local states $l_1,...,l_k$ and global states $b_1,...,b_k$



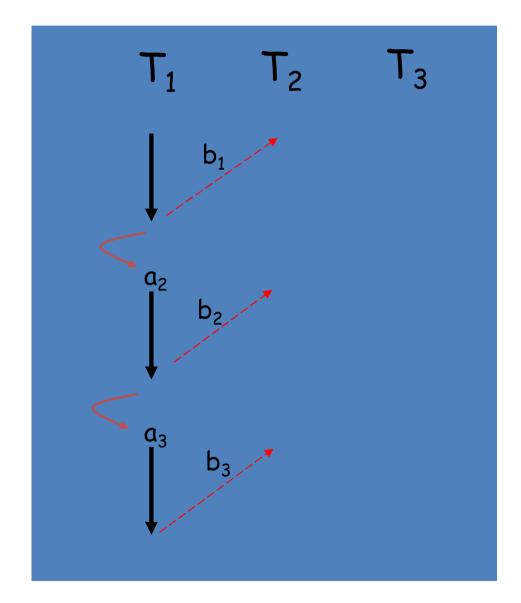
• [Lal-Reps, CAV'08]

- 1. Guess a_2, \ldots, a_k
- 2. Execute T₁ to completion
- 3. Pass b_1, \ldots, b_k to T_2



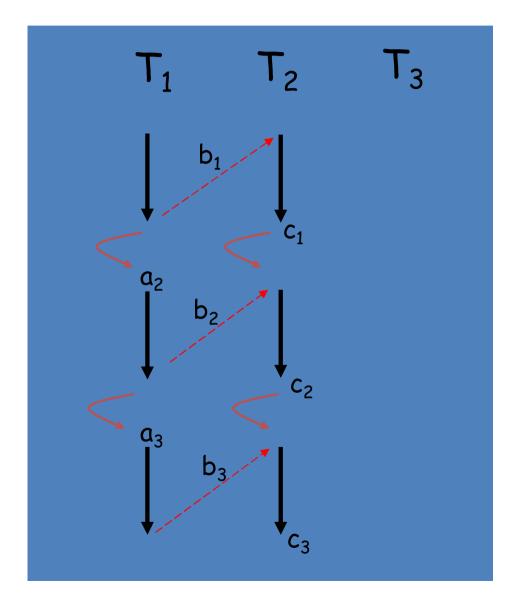
• [Lal-Reps, CAV'08]

- 1. Guess a_2, \ldots, a_k
- 2. Execute T₁ to completion
- 3. Pass b_1, \dots, b_k to T_2
 - □ We can forget of locals



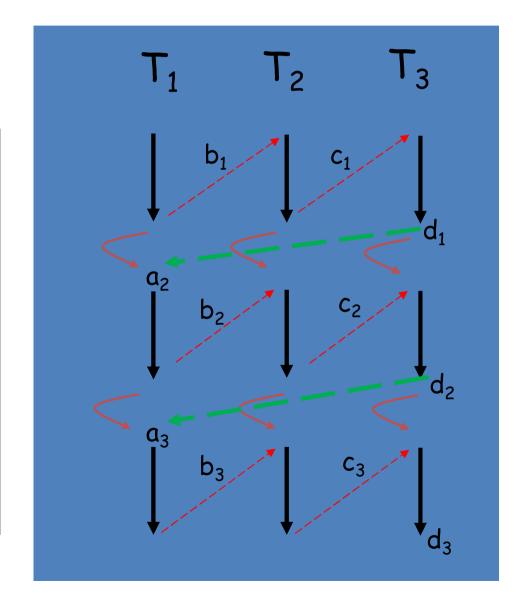
• [Lal-Reps, CAV'08]

- 1. Guess a_2, \ldots, a_k
- 2. Execute T₁ to completion
- 3. Pass b_1, \dots, b_k to T_2
- 4. Execute T₂ to completion



• [Lal-Reps, CAV'08]

- 1. Guess a₂,...,a_k
- 2. Execute T₁ to completion
- 3. Pass $b_1, ..., b_k$ to T_2
- 4. Execute T₂ to completion
- 5. Pass c_1, \dots, c_k to T_3
- 6. Execute T₃ to completion
- 7. Computation iff $d_i = a_{i+1} \forall i \in [1,k-1]$



Translation scheme

Input: concurrent program $P_1,...,P_n$ Output is a sequential program consisting of:

(Seq; is the translation of P_i)

```
\mathbf{Seq}_{1}() \qquad \mathbf{Seq}_{n}()
```

Eager translation (k-rounds)

- 2k-1 copies of shared vars
 - r₂,...,r_k (store guessed starting values)
 - $-s_1,...,s_k$ (copies per round of shared vars)
- main is very simple:

```
guess r<sub>2</sub>,...,r<sub>k</sub>
Seq<sub>1</sub>()
.....
Seq<sub>n</sub>()
Checker()
Error()
```

- Seq_i():
 - code of P_i using the copy s_j at round j
 - implements round-switching by moving to next copy of shared vars
 - returns to main after last round
- Checker():

 for i = 1 to K 1 do
 assume (s_i = r_{i+1})
- Error(): assume(goal)

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Eager seq. does not preserve assertions

```
// shared variables
bool blocked=true;
int x=0, y=0;
```

```
process P1:
   main() begin
   while (blocked)
       skip;
   assert(y!=0);
   x = x/y;
   end
```

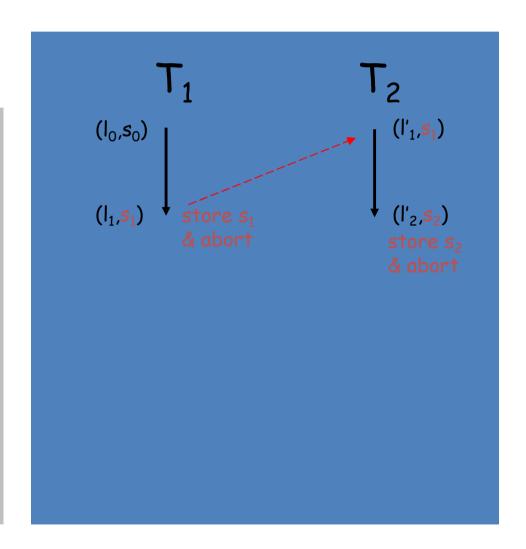
```
process P2:
  main() begin
  x=12;
  y=2;
  //unblock threads of P1
  blocked=false;
  end
```

- y!=0 is an invariant of the statement x=x/y in the concurrent progr.
 - but not in the sequential program
 (blocked can be nondeterministically assigned to false across a context-switch while processing P1)

Lazy transformation: main idea

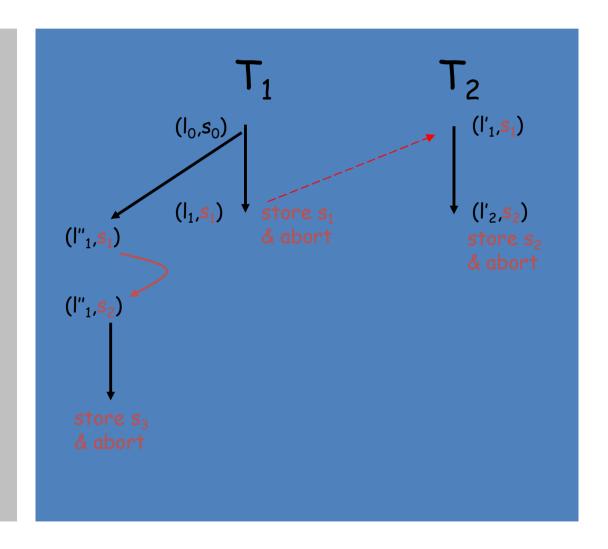
[La Torre-Madhusudan-Parlato, CAV'09]

- □ Execute T₁
- ☐ Context-switch:store s₁ and abort
- Execute T₂ from S₁
- \square store s_2 and abort



Lazy transformation: main idea [La Torre-Madhusudan-Parlato, CAV'09]

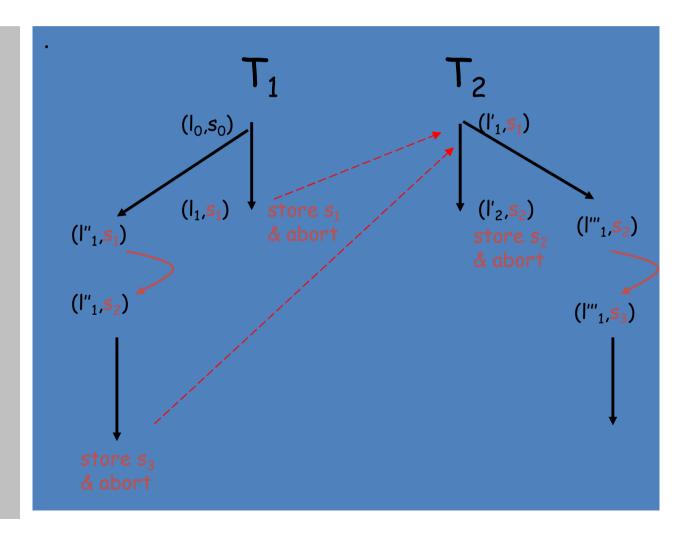
- Re-execute T1 till it reaches s1
 - May reach a new local state!
 - Anyway it is correct !!
- Restart from global s2 and compute s3



Lazy transformation: main idea

[La Torre-Madhusudan-Parlato, CAV'09]

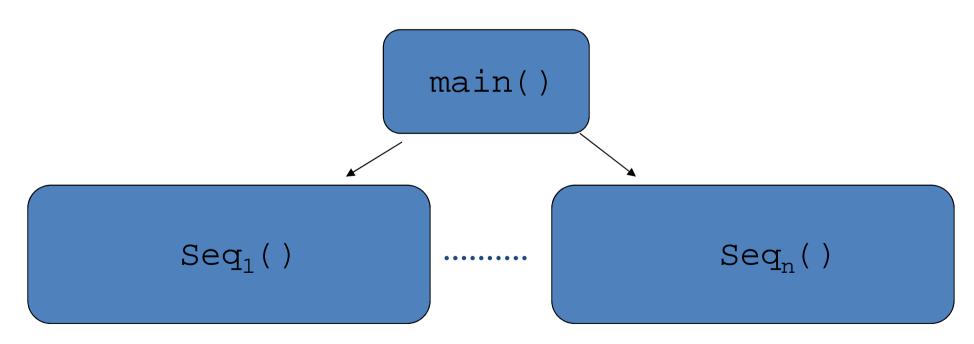
- ☐ Switch to T2
- Execute till it reaches s2
- Continue computation from global s3



Translation scheme (as in Eager)

Input: concurrent program $P_1,...,P_n$

Output is a sequential program consisting of: $(Seq_i \text{ is the translation of } P_i)$



Lazy translation (k-contexts)

- k copies of shared vars
 - $-s_1,...,s_k$ (copies of shared vars to store values at cs)
- main has more control stms:
 - No guessing
 - Keeps track of the current context
 - Starts a thread or its recomputation by assigning the values of sh. vars at first of its contexts

Lazy translation (k-contexts)

- Seq_i():
 - code of P_i interleaved
 with control code

```
if (terminate) then return;
else
  if (*) then call contextSwitch();
  if (terminate) then return;
```

 No special handling of error condition

- contextSwitch()
 - when recomputing contexts:
 - 1. matches values at cs
 - 2. set starting values for next context
 - when context-switching out the currently new computed context
 - 1. stores the sh vars in the appropriate copy
 - 2. set terminate to true

Summarizing lazy translation

- Explores only reachable states
- Preserves invariants across the translation
- Tracks local state of one thread at any time
- Tracks values of shared variables at context switches $(s_1, s_2, ..., s_k)$
- Requires recomputation of local states

Both translations reduce bounded reachability to sequential reachability

Theorem:

Let C be a concurrent program, k>0 and pc be a program counter of C

pc is reachable in C within k context switches iff pc is reachable in $SeqProg_k(C)$

Lazy vs. Eager: performace

- Tool Getafix implements both eager and lazy sequentialization for concurrent Boolean programs
- Lazy outperforms Eager in the experiments
- Sample results on Windows NT Bluetooth driver

Context switches	1-adder 1-stopper			2-adders 1-stopper			1-adder 2-stoppers			2-adders 2-stoppers		
		eager	lazy		eager	lazy		eager	lazy		eager	lazy
1	Ν	0.1	0.1	Ν	0.2	0.1	Ν	0.1	0.1	Ν	0.2	0.1
2	Ν	0.3	0.2	Ν	0.9	0.8	Ν	0.7	0.9	Ν	1.6	2.0
3	Ν	43.3	1.4	Ν	135.9	6.3	Υ	70.1	0.4	Υ	177.6	0.8
4	Ν	73.6	5.5	Υ	1601.0	2.6	Υ	597.2	2.9	Υ	out of mem.	7.5
5	Ν	930.0	20.2	Υ	-	18.0	Υ	-	14.0	Υ	out of mem.	66.5
6	N	-	66.8	Υ	-	122.9	Υ	-	66.1	Υ	out of mem.	535.9

Lazy vs. Eager: performace

- Getafix uses as verification engine a fixed-point logic solver (Mucke)
 - It stores summaries, recomputations do not cause to repeat exploration
 - Explore the state space lazily gives some advantages
- Experiments using BMC (Bounded Model-checking) backends gives the opposite result
 - Eager outperforms Lazy
 [Ghafari-Hu-Rakamaric, SPIN'10]

Tools implementing LR seq.



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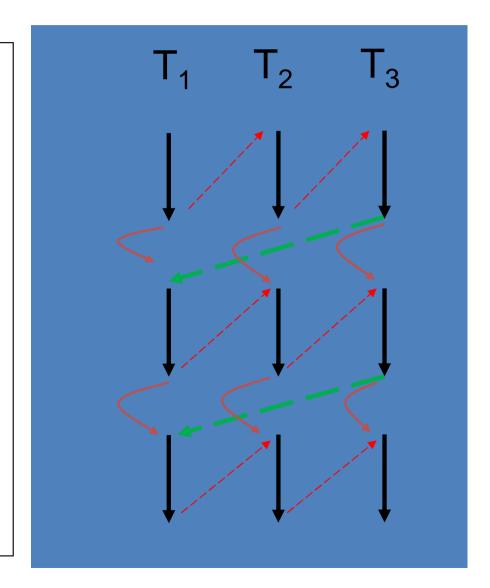
Parameterized programs

- Extend shared-memory concurrent programs
 - Computations can have an arbitrary number of threads
- Complex class of programs (infinite states):
 - each thread can have recursive calls
 - number of threads is unbounded
- Interesting class of programs (e.g., device drivers)
 - can be used to analyze programs with dynamic thread creation

Sequentialization of param. progs

[La Torre-Madhusudan-Parlato, FIT'12]

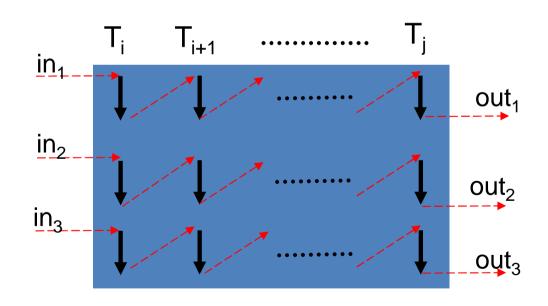
- Eager sequentialization can be easily obtained from that for concurrent programs:
 - each thread is executed up to completion (jumping across contextswitches)
 - after computing a thread, nondeterministically (1) terminate and check if all the computed executions form a computation and (2) compute next thread
 - the values of shared variables at context-switches are passed to the next thread



Linear interfaces

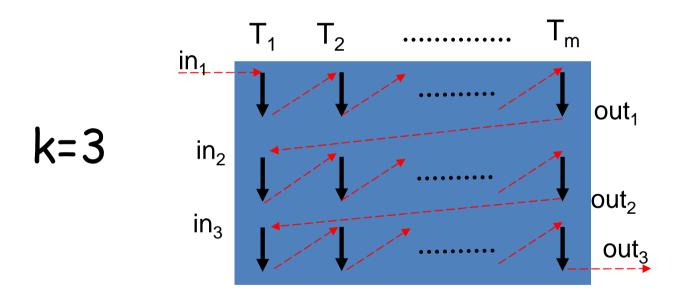
- Summarize the effects of a block of unboundedly many threads on the shared variables
 - executions arranged in rounds of round-robin scheduling

linear interface (In,Out) of dim. 3



Linear interface of a run

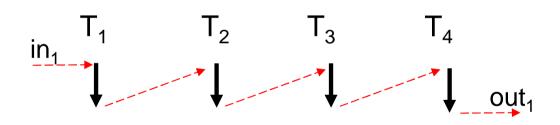
• (In,Out) s.t. $in_{i+1}=out_i$ i=1,...,k-1



Lazy sequentialization

[La Torre-Madhusudan-Parlato, FIT'12]

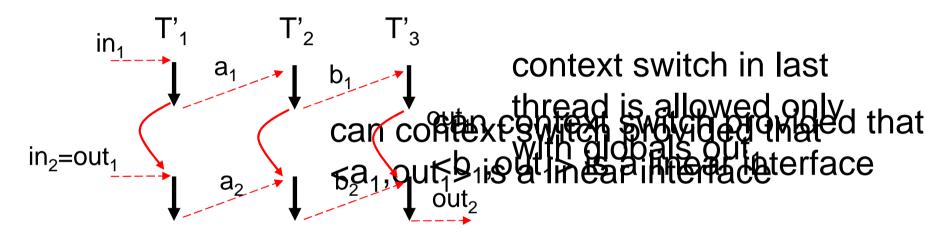
- P_{seq} mimics a computation of P
 - by increasing round numbers and
 - (within each round) by increasing context numbers



- nondeterministically chooses if this is the last thread in the round
- the linear interface (<in₁>,<out₁>) is stored

Lazy sequentialization

Second round is executed matching (<in₁>,<out₁>)



- Note that threads do not need to be the same we used in the first round and not even in the same number
- The third round is executed similarly by matching (\(\in_1\),in₂\(\times\),\(\cdot\)

Dynamic thread creation

- New threads can be istantiated at runtime (e.g., thread creation, asynchronous calls)
- Computations may have unboundedly many threads running at the same time
- Main idea to handle dynamic creation:
 - schedule threads according to a (DFS) visit of the ordered thread-creation tree
 - this allows to use the call stack to explore the pending threads
- This nicely combines with the Eager scheme

Delay-bounded scheduling

[Emmi-Qadeer-Rakamaric, POPL'11]

- Programs with asynchronous calls (creating tasks)
- Each task is executed to completion (no interleaving with other tasks)
- Sequentialization is according to a DFS scheduler of tasks
- When dispatched, a task can be delayed to next round
 - the total number of delays in a task-creation tree is bounded by k
 - total number of explored rounds is k+1
- The beginning of each round is guessed (eager)

General sequentialization

[Bouajjani-Emmi-Parlato, SAS'11]

- Programs with asynchronous calls
- Tasks can be interleaved with other ones
- Sequentialization based on generalization of Linear Interfaces
 - DAGs of contexts
 - Composition and compression operations
- Bound on the size of the DAGs
- Generalizes k-rounds Eager e delay boundedscheduling sequentialization

Scope-bounded sequentialization [La Torre-Napoli-Parlato, DLT'14] [La Torre-Parlato, FSTTCS'12]

- No dynamic thread creation
- k-scoped generalizes k-context analysis
 - bounds the number of times a thread is suspended/resumed between each matching call and returns
- Each scope is captured by a linear interface
- Sequentialization mantains a set of linear interfaces (one for each thread)
- Each thread contributes with many LI's in a computation
- Both Eager and Lazy schemes

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Conclusion

- Sequentialization is an effective approach to analyze concurrent programs
- Main features:
 - Fast prototyping
 - Re-use of mature technologies (tools for sequential programs)
 - Code-to-code translation
 - Introduces some overhead (variables, control code, recursive calls)

Conclusion

- Presented translations:
 - keep track only of the local state of the current thread (no cross product)
 - except for KISS, use # copies of the shared variables depending on the bounding parameter
 - thread creation is implemented with calls
- Eager translations require guessing of values of the shared variables and explore unreachable states
- Lazy translations preserve the invariants and introduces many recursive calls (re-computations)

Conclusions

- Experiments show:
 - Exploring only reachable states impacts positively the size of BDD's in the Getafix approach
 - Recursive calls impacts negatively the size of formulas in Bounded Model-Checking backends
- Sequentialization schemes should be targeted to a class of backends

Talk on June 5

- Sequentializations for Bounded Model Checking backends
- Tool CSeq http://users.ecs.soton.ac.uk/gp4/cseq/cseq.html
- Based on joint work with Bernd Fischer, Omar Inverso, Gennaro Parlato and Ermenegildo Tomasco
 - TACAS-SVCOMP'14, CAV'14 and on-going research